



# The Effect of Data Point Censoring on Correlations Between Skewed Variables

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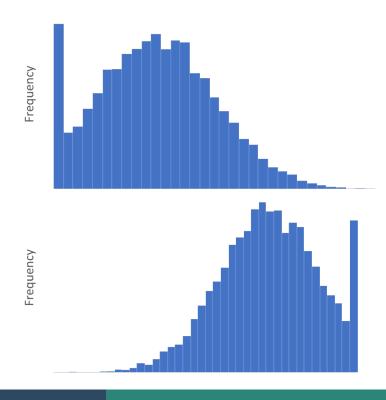
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#### **Data Point Censoring**

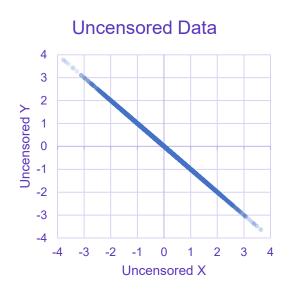
Data point censoring occurs when a researcher knows a value is at least as large as (or no larger than) a certain value

- Left censoring
  - Value is too small to be detected
  - Floor effects
- Right censoring
  - Length of time to event or frequency of event is underestimated
  - Ceiling effects

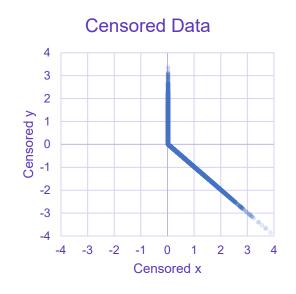




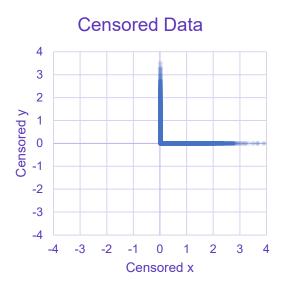
#### Censoring Distorts Correlations



X and Y have bivariate normal distribution with  $\rho_{XY} = -1$ 



Half the x values are censored. If X < 0, x = 0.



Half the y values are also censored.

$$\rho_{xy} = -.467$$

(Russell & Carroll, 1999)



## We Examined the Effect of Left Censoring on Correlations for Skewed Data

24 datasets with 50,000 cases

Correlations: .7 and -.7

Skew: .5 and -.5

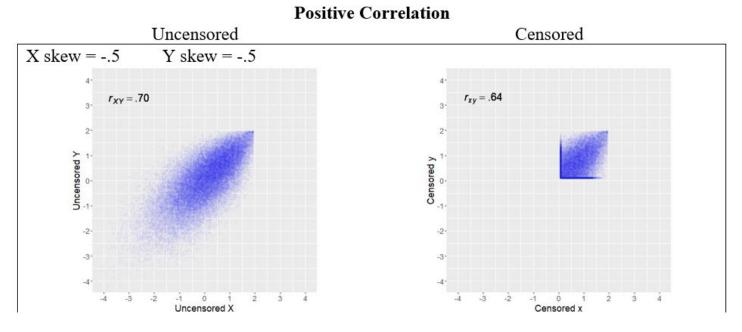
Left censoring: 30%, 50%, 70%

One of our datasets:

50% censoring on x 50% censoring on y

$$\rho_{XY} = .70$$

$$\rho_{\chi\gamma} = .64$$





#### Our 24 Datasets

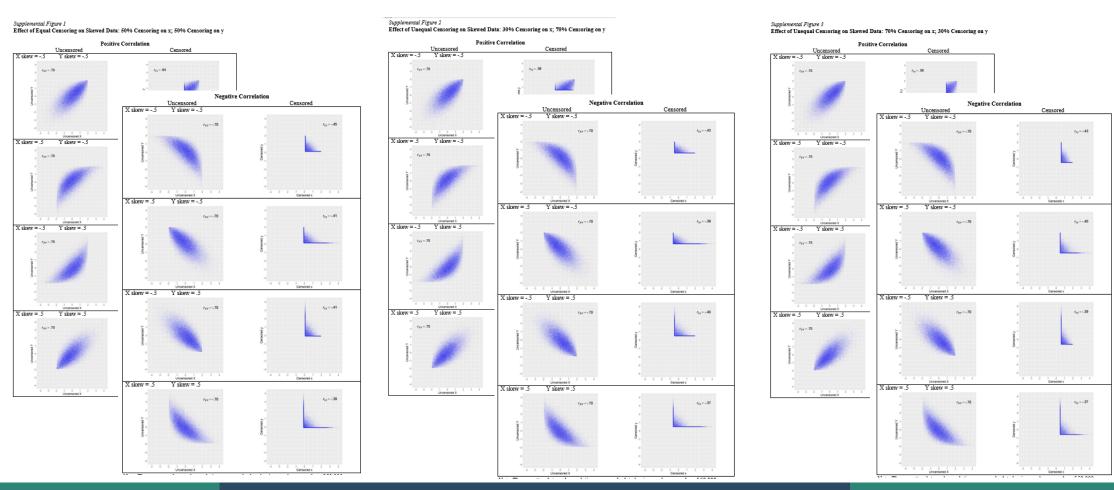
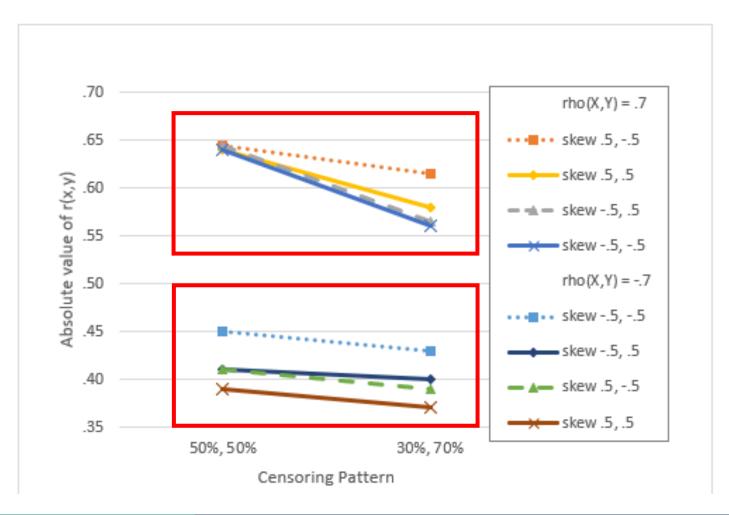


Figure 1

Three-way Interaction of rho(X,Y), Censoring Pattern, and Skew on r(x,y)

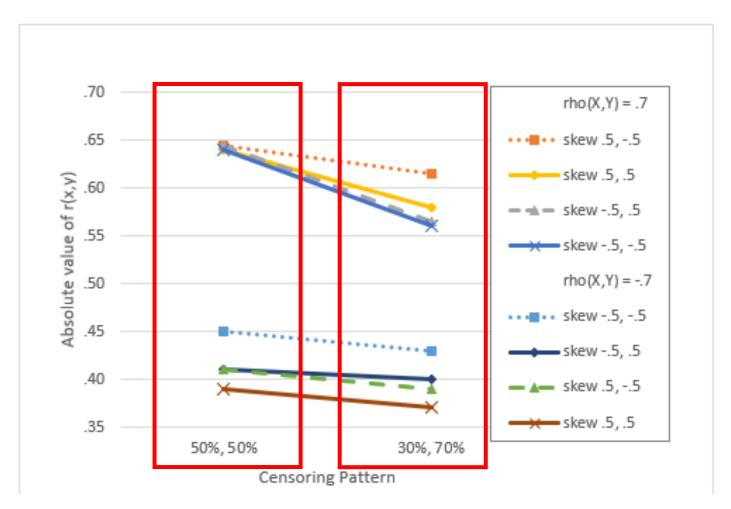


## Main Effect for Correlation

Left censoring affects negative correlations more than positive correlations.

Figure 1

Three-way Interaction of rho(X,Y), Censoring Pattern, and Skew on r(x,y)

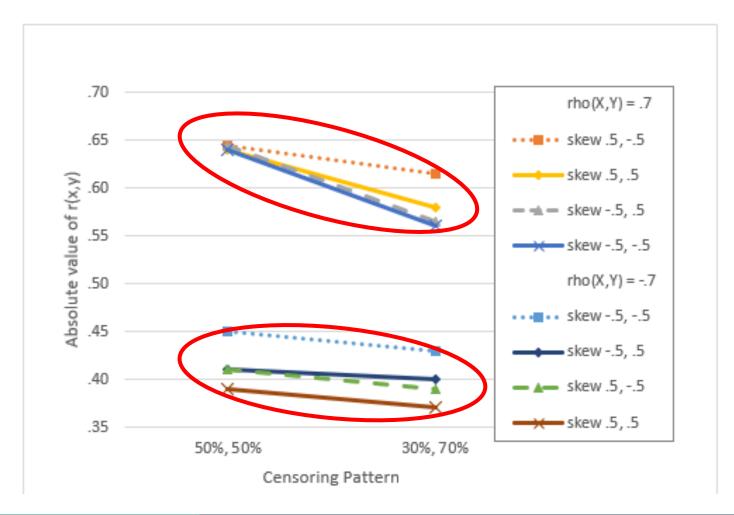


## Main Effect for Censoring Pattern

Unequal censoring has a greater effect than equal censoring.

Figure 1

Three-way Interaction of rho(X,Y), Censoring Pattern, and Skew on r(x,y)

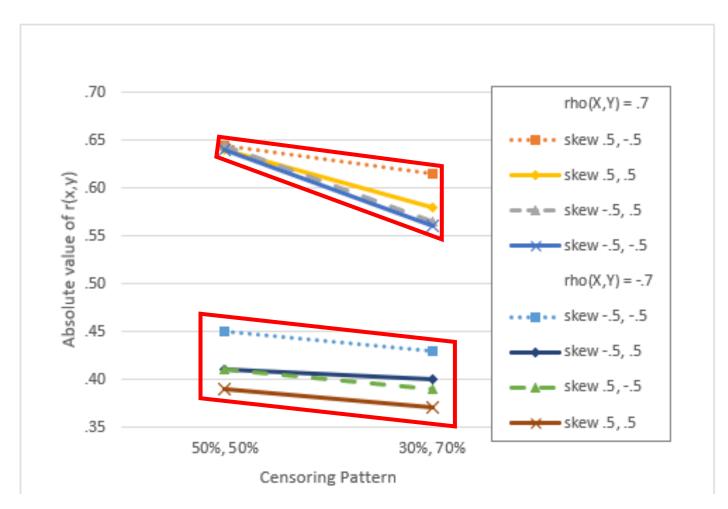


## Interaction of Censoring Pattern and Correlation

Unequal <u>left</u>
censoring has
bigger effect on
<u>positive</u>
correlations than
negative ones.

Figure 1

Three-way Interaction of rho(X,Y), Censoring Pattern, and Skew on r(x,y)



## Three Way Interaction

For <u>left</u> censoring, censoring pattern and skew interact more for <u>positive</u> correlations than negative ones.



#### Discussion

- Right censoring is the mirror image of left censoring. Therefore,
  - If both variables have right censoring
    - Unequal censoring has a greater effect than equal censoring.
    - Censoring affects <u>negative</u> correlations more than positive ones.
    - Censoring pattern and skew interact more for <u>positive</u> correlations than negative.
  - If one variable has left censoring and one has right censoring
    - Unequal censoring has a greater effect than equal censoring.
    - Censoring affects positive correlations more than negative ones.
    - Censoring pattern and skew interact more for <u>negative</u> correlations than positive.
- A variety of methods (e.g., Mplus, R package lava) use data from censored variables to estimate correlations for uncensored variables.
  - Future research: How well do they work with skewed data?